

# Package ‘qcluster’

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**Title** Clustering via Quadratic Scoring

**Description** Performs tuning of clustering models, methods and algorithms including the problem of determining an appropriate number of clusters. Validation of cluster analysis results is performed via quadratic scoring using resampling methods, as in Coraggio, L. and Coretto, P. (2023) <[doi:10.1016/j.jmva.2023.105181](https://doi.org/10.1016/j.jmva.2023.105181)>.

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banknote	<i>Swiss Banknotes Data</i>
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### Description

Data from Tables 1.1 and 1.2 (pp. 5-8) of Flury and Riedwyl (1988). There are six measurements made on 200 Swiss banknotes (the old-Swiss 1000-franc). The banknotes belong to two classes of equal size: *genuine* and *counterfeit*.

### Format

A data.frame of dimension 200x7 with the following variables:

**Class** a factor with classes: genuine, counterfeit

**Length** Length of bill (mm)

**Left** Width of left edge (mm)

**Right** Width of right edge (mm)

**Bottom** Bottom margin width (mm)

**Top** Top margin width (mm)

**Diagonal** Length of diagonal (mm)

### Source

Flury, B. and Riedwyl, H. (1988). *Multivariate Statistics: A practical approach*. London: Chapman & Hall.

bqs

*Bootstrapping quadratic scores***Description**

Estimates the expected quadratic score for clustering solutions provided by a list of candidate models, methods or algorithmic settings.

**Usage**

```
bqs(
  data,
  methodset,
  B = 10,
  type = "smooth",
  oob = FALSE,
  ncores = detectCores() - 2,
  alpha = 0.05,
  rankby = ifelse(B == 0, "mean", "lq"),
  boot_na_share = 0.25,
  savescores = FALSE,
  saveparams = FALSE
)
```

**Arguments**

data	a numeric vector, matrix, or data frame of observations. Rows correspond to observations and columns correspond to variables/features. Categorical variables and NA values are not allowed.
methodset	a function, a list of functions, or a qcmethod object. Each method takes data as input and provides a clustering solution to be scored (see <i>Details</i> ). See also <code>mset_*</code> ( <code>)</code> helpers and <code>mbind</code> .
B	an integer $\geq 0$ . If $B=0$ , methods are fitted and scored on the full data without resampling. If $B \geq 1$ , B is the number of bootstrap replicates (see <i>Details</i> ).
type	character string in <code>c("smooth", "hard", "both")</code> . "smooth" (default) estimates only the smooth score, "hard" only the hard score, and "both" estimates both.
oob	logical or character string in <code>c(FALSE, TRUE, "only")</code> . FALSE (default) skips out-of-bag scoring, TRUE adds it to the empirical bootstrap scoring, and "only" computes only the out-of-bag scores.
ncores	an integer, it defines the number of cores used for parallel computing (see <i>Details</i> ). Setting <code>ncores = 0</code> uses all detected cores.
alpha	a number in $(0, 1)$ , the confidence-level for empirical bootstrap quantiles (both-tails).

rankby	character string in c("lq", "mean", "1se") or NA to skip ranking. "lq" (default) maximizes the lower limit of the $1-\alpha$ bootstrap confidence interval, "mean" maximizes the estimated expected score, and "1se" maximizes the lower limit of a confidence interval whose semi-length is one estimated standard error.
boot_na_share	a numeric value in $(0, 1)$ . During the bootstrapping a method's score is set to NA if the underlying computation runs into errors. Methods resulting in more than $B * \text{boot\_na\_share}$ errors are excluded from the comparison.
savescores	logical, if =TRUE it returns estimated scores for each bootstrap sample.
saveparams	logical, if =TRUE it returns estimated cluster parameters for each bootstrap sample.

## Details

The function implements the estimation and selection of an appropriate clustering based on the methodology proposed in Coraggio and Coretto (2023). It also allows out-of-bag score estimates alongside the empirical bootstrap estimates considered in that paper. Since out-of-bag estimates reuse the same bootstrap samples, `oob=TRUE` adds only a small extra cost. Setting `B=0` gives a no-resampling baseline rather than a bootstrap estimate.

**Choice of B.** In theory B should be as large as possible, however, if the list of methods is large and the computational capacity is modest, a large B may require long run times. Coraggio and Coretto (2023) show experiments where changing from `B=1000` to `B=100` introduces a marginal increase in variability. `B=100` should be considered as a lower bound. In the case where one has very large method lists, high-dimensional datasets and demanding methods, a possible strategy to reduce the computational cost is as follows:

1. set a small value of B, e.g., `B=50` or even less.
2. Analyze the methods' ranking and identify those methods that report score values that are small compared to the top performers.
3. Narrow down the methodset list and repeat the bootstrap estimation with a value of B that is as large as possible relative to available computational resources.

**Parallel computing.** Bootstrap sampling is performed using foreach-based parallel computation via the `doParallel` parallel backend. Note that depending on the system settings, and how the functions in `methodset` make use of parallelism and/or multi-threading computing, increasing `ncores` may not produce the desired reduction in computing time. A common source of inefficiency is nested parallelism: `foreach` distributes work across R workers while linear algebra libraries (e.g., OpenBLAS, Intel Math Kernel Library (MKL), BLIS, Accelerate) also start their own threads inside each worker. By default, `bqs` avoids this oversubscription by forcing each worker to use a single BLAS/OpenMP thread whenever process-level parallelism is active.

**methodset argument.** The `methodset` argument allows in input a function, list, or output from `mset` functions: `mset_user`, `mset_gmix`, `mset_kmeans`, `mset_pam`. It is also possible to give any combination of these, concatenated with the `mbind` function. When passing a function, either as a single element or in a list, this must take the data set as its first argument, and must return in output at least a list named `"params"`, conforming with the return value of `clust2params`, i.e. a list containing `proportion`, `mean` and `cov` elements, representing the estimated clusters' parameters.

When `rankby` is not NA, the `best_*` components are computed by re-estimating the selected method on the full data set. For stochastic methods, use `set.seed()` if reproducibility is required.

**Value**

An S3 object of class `bqs`. The exact components depend on `type`, `oob`, `rankby`, `savescores`, and `saveparams`.

Any available score summary among `smooth`, `hard`, `oob_smooth`, and `oob_hard` is a data frame with one row per method and columns:

`id` index of the method in `methodset`;  
`rank` rank according to `rankby`;  
`mean` estimated expected score;  
`sterr` standard error of the mean score;  
`lower_qnt` lower confidence limit for the mean score;  
`upper_qnt` upper confidence limit for the mean score;  
`n_obs` number of valid bootstrap samples;  
`n_missing` number of filtered erroneous cases.

Other output components are:

**smooth** returned if `type="smooth"` or `type="both"`.

**hard** returned if `type="hard"` or `type="both"`.

**oob\_smooth** returned if `type="smooth"` or `type="both"` and `oob=TRUE` or `oob="only"`.

**oob\_hard** returned if `type="hard"` or `type="both"` and `oob=TRUE` or `oob="only"`.

**best\_smooth** list with components `method_name` and `solution` for the best smooth-scoring method. Returned only when ranking is available and a rank-1 solution exists.

**best\_hard** analogous object for the hard score.

**best\_oob\_smooth** analogous object for the out-of-bag smooth score.

**best\_oob\_hard** analogous object for the out-of-bag hard score.

**data** a list containing information about the input data set necessary for the fruition of the returned object.

**B** number of bootstrap replicates.

**methodset** the elements of `methodset` for which a solution is produced.

**rankby** the ranking criterion.

**raw** a list returned if `savescores=TRUE` and/or `saveparams=TRUE`. Let  $n$ =sample size,  $B$ =bootstrap samples,  $M$ = number of methods in `methodset`. It may contain:

**boot\_id**: an array of dimension  $n \times B$  where the  $j$ -th column contains the indexes of the observed data points belonging to the  $j$ -th bootstrap sample. That is, `data[boot_id[, j], ]` gives the  $j$ -th bootstrap data set.

**scores**: an array of dimension  $(M \times 3 \times B)$  returned if `savescores=TRUE`. It stores error codes and hard/smooth scores for each bootstrap replicate.

**oob\_scores**: returned if `oob=TRUE` or `oob="only"` and `savescores=TRUE`. It is an array organized as the previous object `scores`, but for out-of-bag estimates.

**params**: a list returned if `saveparams=TRUE`. `params[[m]]` contains estimated cluster parameters for `methodset[[m]]` where  $m=1, \dots, M$ . Each member of the list is a list of length  $B$  where `params[[m]][[b]]` contains the cluster parameters fitted by the  $m$ -th method on the  $b$ -th bootstrap sample.

## References

Coraggio, Luca and Pietro Coretto (2023). Selecting the number of clusters, clustering models, and algorithms. A unifying approach based on the quadratic discriminant score. *Journal of Multivariate Analysis*, Vol. 196(105181), 1-20. doi: [doi:10.1016/j.jmva.2023.105181](https://doi.org/10.1016/j.jmva.2023.105181)

## See Also

[mset\\_user](#), [mset\\_gmix](#), [mset\\_kmeans](#), [pam](#), [mbind](#), [clust2params](#)

## Examples

```
# load data
data("banknote")
dat <- banknote[-1]

## set up methods
## see also help('mset_user') and related functions
KM <- mset_kmeans(K = 3)
GMIX <- mset_gmix(K = 3, erc = c(1, 100))

# combine tuned methods
mlist <- mbind(KM, GMIX)

# perform bootstrap
# change B and ncores to a much larger value in real problems
res <- bqs(dat, mlist, B = 3, type = "both", rankby = "lq",
          ncores = 1, oob = TRUE, savescores = TRUE, saveparams = FALSE)
names(res)
res

## Not run:
# The following example is more realistic but may take time
# -----
# load data
data("banknote")
dat <- banknote[-1]

# set up kmeans, see help('mset_kmeans')
KM <- mset_kmeans(K = 2:5)

# set up Gaussian model-based clustering via gmix()
GMIX <- mset_gmix(K = 2:5, erc = c(1, 50, 100))

# set up Gaussian model-based clustering via library("mclust")
# see examples in help('mset_user')
require(mclust)
mc_wrapper <- function(data, K, ...){
  y <- Mclust(data, G = K, ...)
  y[["params"]] <- list(proportion = y$parameters$pro,
                      mean = y$parameters$mean,
                      cov = y$parameters$variance$sigma)
  return(y)
}
```

```

}
MC <- mset_user(fname = "mc_wrapper", K = 2:5,
               modelNames = c("EEI", "VVV"))

# combine tuned methods
mlist <- mbind(KM, GMIX, MC)

# perform bootstrap
# set 'ncores' to the number of available physical cores
res <- bqs(dat, mlist, B = 100, type = "both", rankby = "lq", ncores = 1,
          oob = TRUE, savescores = TRUE, saveparams = FALSE)

res

## End(Not run)

```

---

bqs\_rank

*Ranking Clusters Quadratic Scores Estimated Via Bootstrap*


---

## Description

Ranks the scores of clustering methods estimated via bootstrap.

## Usage

```
bqs_rank(bqsol, rankby = "lq", boot_na_share = 0.25)
```

## Arguments

bqsol	an object of class bqs obtained from <a href="#">bqs</a> .
rankby	character string specifying how the scored solutions are ranked. Possible values are {"lq", "mean", "1se"}. With "lq" (default), the solutions are ranked by maximizing the estimated lower limit of the 1-alpha bootstrap confidence interval for the expected score. With "mean", the solutions are ranked by maximizing the estimated expected score. With "1se", the solutions are ranked by maximizing the estimated lower limit of the confidence interval for the expected score whose semi-length is equal to a <i>standard error</i> . The expected score's <i>standard error</i> is approximated using the bootstrap distribution. See <i>Details</i> for small-B behavior.
boot_na_share	a numeric value in [0, 1]. During the bootstrapping a method's score is set to NA if the underlying computation runs into errors. Methods resulting in more than B * boot_na_share errors are excluded from the comparison.

## Details

For small B, some ranking criteria may be unstable or unavailable. In particular, with B=1, "lq" is effectively equivalent to "mean", while "1se" is not computable and the corresponding ranks remain NA. For B<5 warns that "lq" and "1se" may yield imprecise estimates.

**Value**

An S3 object of class `bqs`. Output components are those of `bqs`. The score-summary components are re-ranked in place. Any stored `best_*` components are refreshed and are returned only when a rank-1 solution exists under the new ranking. See *Value* in `bqs`. The object is modified only in its ranking-related components.

**References**

Coraggio, Luca and Pietro Coretto (2023). Selecting the number of clusters, clustering models, and algorithms. A unifying approach based on the quadratic discriminant score. *Journal of Multivariate Analysis*, Vol. 196(105181), 1-20. doi: [doi:10.1016/j.jmva.2023.105181](https://doi.org/10.1016/j.jmva.2023.105181)

**See Also**

[bqs](#), [bqs\\_select](#)

**Examples**

```
# load data
data("banknote")
dat <- banknote[-1]

## set up methods
## see also help('mset_user') and related functions
KM <- mset_kmeans(K = 3)
GMIX <- mset_gmix(K = 3, erc = c(1, 100))

# combine tuned methods
mlist <- mbind(KM, GMIX)

# perform bootstrap
# change B and ncores to a much larger value in real problems
res <- bqs(dat, mlist, B = 3, rankby = "lq", ncores = 1)
res

# now change ranking criterion
res2 <- bqs_rank(res, rankby = "mean")
res2
```

---

bqs\_select

*Select Ranked Cluster Solutions by Quadratic Score*

---

**Description**

Select solutions from a `bqs` object based on specified rank and type of score.

**Usage**

```
bqs_select(
  bqs_sol,
  rank = 1,
  type = "smooth",
  rankby = NA,
  boot_na_share = 0.25
)
```

**Arguments**

bqs_sol	An object of class bqs containing the clustering solutions to be selected.
rank	An integer $>0$ specifying the rank of the solution to select. Default is 1.
type	A character string specifying the type of Quadratic Score. Possible values are "hard", "smooth", "oob_hard", "oob_smooth". Default is "smooth".
rankby	A character string specifying the criteria used to rank solutions in bqs. Possible values are "lq", "mean", "1se", or NA (default). See <i>Details</i> .
boot_na_share	A numeric value between $[0, 1]$ . Clustering solutions in bqs_sol with a share of NA bootstrap estimates are excluded from ranking. Default is 0.25.

**Details**

Even if the bqs\_sol object is not pre-ranked, the user may specify a ranking criterion to rank clustering solutions dynamically using the rankby argument; this does not modify the original bqs\_sol object. In these instances, the user can also specify boot\_na\_share as in [bqs\\_rank](#) to exclude solutions based on the proportion of unsuccessful bootstrap estimations. If rankby=NA, the bqs\_sol must be pre-ranked.

Selected solutions are always re-estimated on the full dataset before being returned. Therefore, for stochastic clustering methods, repeated calls may return different fitted solutions unless the user controls reproducibility, e.g. via `set.seed()`.

**Value**

A named list of all clustering solutions achieving a type score of rank rank when ranked according to rankby criterion, or NULL if no such solution is available in the bqs\_sol object. List names correspond to methods' names in bqs\_sol\$methodset. Each named entry contains the corresponding method re-estimated on bqs\_sol\$data\$data. If the full-data refit fails, the corresponding entry is an object of class bqs\_select\_error containing the failure status and message. If the requested rank exceeds the largest available rank, the worst available rank is returned instead. If the requested rank is within range but absent because of rank gaps, NULL is returned.

**See Also**

[bqs](#), [bqs\\_rank](#)

**Examples**

```

# Load data and set seed
set.seed(123)
data("banknote")
dat <- banknote[-1]

# set up kmeans, see help('mset_kmeans')
KM <- mset_kmeans(K = 2:5)

# set up Gaussian model-based clustering via gmix()
GMIX <- mset_gmix(K = 2:5, erc = c(1, 50, 100))

# combine tuned methods
mlist <- mbind(KM, GMIX)

# perform bootstrap
# set 'ncores' to the number of available physical cores
res <- bqs(dat, mlist, B = 20, type = "both", rankby = NA, ncores = 1,
          oob = TRUE, savescores = TRUE, saveparams = FALSE)

# Methods are not ranked; this will raise an error
try(bqs_select(res, rank = 1))

# Rank method dynamically
ranked_res <- bqs_select(res, rank = 2, rankby = "lq",
                        boot_na_share = 0.25)

names(ranked_res)

```

---

clust2params

*Converts Hard Assignment Into Cluster Parameters*


---

**Description**

Transforms cluster labels into a list of parameters describing cluster size, mean, and dispersion.

**Usage**

```
clust2params(data, cluster)
```

**Arguments**

data	a numeric vector, matrix, or data frame of observations. Rows correspond to observations and columns correspond to variables/features. Categorical variables and NA values are not allowed.
cluster	a vector of integers representing cluster labels. Labels need not be consecutive.

**Value**

A list containing cluster parameters, conformable with the Gaussian parameterization used by functions such as `qscore`. Let  $P$ =number of variables/features and  $K$ =number of clusters. The elements of the list are as follows:

- `proportion`: a vector of clusters' proportions;
- `mean`: a matrix of dimension  $(P \times K)$  containing the clusters' mean parameters;
- `cov`: an array of size  $(P \times P \times K)$  containing the clusters' covariance matrices.

**Examples**

```
# load data
data("banknote")

# compute the k-means partition
set.seed(2024)
cl <- kmeans(banknote[-1], centers = 2, nstart = 1)$cluster

# convert k-means hard assignment into cluster parameters
clpars <- clust2params(banknote[-1], cl)
clpars
```

---

gmix

*Gaussian Mixture Modelling*

---

**Description**

Fast implementation of the EM algorithm for ML estimation and clustering of Gaussian mixture models with covariance matrix regularization based on eigenvalue ratio constraints.

**Usage**

```
gmix(
  data,
  K = NA,
  erc = 50,
  iter.max = 1000,
  tol = 1e-08,
  init = "kmed",
  init.nstart = 25,
  init.iter.max = 30,
  init.tol = tol,
  save_cluster = TRUE,
  save_params = TRUE,
  save_taus = FALSE
)
```

## Arguments

<code>data</code>	a numeric vector, matrix, or data frame of observations. Rows correspond to observations and columns correspond to variables/features. Let $N = \text{nrow}(\text{data})$ and $P = \text{ncol}(\text{data})$ . Categorical variables and NA values are not allowed.
<code>K</code>	the number of mixture components or clusters. It can be left NA only when <code>init</code> is a vector of initial labels, in which case the number of clusters is retrieved from the initial partition. For character, matrix/data frame, and function initializations, <code>K</code> must be supplied.
<code>erc</code>	a numeric value $\geq 1$ specifying the eigenvalue ratio constraint (see <i>Details</i> ).
<code>iter.max</code>	maximum number of iterations for the EM algorithm.
<code>tol</code>	tolerance for the convergence of the EM algorithm.
<code>init</code>	a character in the set <code>c("kmed", "kmeans", "pam")</code> , a vector, a matrix, a data frame, or a callable giving the initial assignment of data points (see <i>Details</i> ). The default choice is "kmed".
<code>init.nstart</code>	number of initial partitions (see <i>Details</i> ).
<code>init.iter.max</code>	maximum number of iterations for each run of the k-median initialization.
<code>init.tol</code>	tolerance for the convergence of each run of the k-median initialization.
<code>save_cluster</code>	logical, if TRUE the point-to-cluster assignment based on the <i>maximum a posteriori probability</i> (MAP) rule is returned.
<code>save_params</code>	logical, if TRUE the estimated mixture parameters are returned.
<code>save_taus</code>	logical, if TRUE the posterior class probabilities are returned (these are also known as <i>posterior weights</i> or <i>fuzzy weights</i> ).

## Details

The function implements the constrained ML estimator studied in Coretto and Hennig (2023). The covariance matrix constraints are computed according to the CM1-step of Algorithm 2 of Coretto and Hennig (2017). This function uses highly optimized C code for fast execution. The constrained M-step extensively uses low-level common linear algebra matrix operations (BLAS/LAPACK routines). Consequently, to maximize computational efficiency, it is recommended that the best available shared libraries, such as OpenBLAS, Intel Math Kernel Library (MKL), etc., be set up.

**Initialization.** The default method, set with `init="kmed"`, uses a fast C implementation of the k-medians algorithm with random initial centers drawn uniformly over the data rows `init.iter.max` times. Depending on the computer power available it is suggested to set `init.iter.max` as large as possible particularly in cases where the data set dimensionality is large in terms of both sample size and number of features. Setting `init="kmeans"` replaces the k-medians with the k-means. With `init="pam"` initial clusters are determined using the PAM algorithm based on Euclidean distances. The latter does not perform multiple starts. The user can also set `init = x` where `x` is a vector of integers of length  $N = \text{nrow}(\text{data})$  representing an initial hard assignment of data points to the mixture components or clusters (see *Examples*). Another possibility is to set `init = W` where `W` is a matrix or data frame of dimension  $(N \times K)$  containing initial posterior probabilities or initial non-negative weights. The assignment provided via `W` can be hard (0-1 weights with the constraint that only a 1 is possible in each row of `W`) or smooth. In the current implementation, entries of `W` must be finite and non-negative, and each cluster must receive positive total weight. `W` can be seen as the initial

version of the object posterior described in the *Value* section above. The last alternative is to set `init = f` where `f` is a function with signature `function(data, K)` returning an  $N \times K$  matrix of initial hard/smooth assignments as described for `W` above (see the example below).

**Eigenvalue ratio constraint** (`erc`). It is the maximum allowed ratio between within-cluster covariance matrix eigenvalues. It defines the so-called *eigenratio constraint*. `erc=1` enforces spherical clusters with equal covariance matrices. A large `erc` allows for large between-cluster covariance discrepancies. It is suggested to never set `erc` arbitrarily large; its main role is to prevent degenerate covariance parameters and the related emergence of spurious clusters (see *References* below). Finally, in order to facilitate the setting of `erc`, it is suggested to scale the columns of data whenever measurement units of the different variables are grossly incompatible.

## Value

An S3 object of class `"mbcfit"`. Output components are as follows:

**info** a list with two components named `code` and `flag` giving information about the underlying EM algorithm. The code objects can take the following values:

- `code=1`: the algorithm converged within `iter.max`.
- `code=2`: the algorithm reached `iter.max`.
- `code=3`: the algorithm did not move from initial values.
- `code=-1`: unexpected memory allocation issues occurred.
- `code=-2`: unexpected LAPACK routine errors occurred.

The `flag` objects can take the following values:

- `flag=0`: no flag.
- `flag=1`: numerically degenerate posterior probabilities could not be prevented.
- `flag=2`: the ERC was enforced at least once.
- `flag=3`: conditions of `flag=1` and `flag=2` occurred.

**iter** number of iterations performed in the underlying EM algorithm.

**N** number of data points.

**P** data dimension.

**K** number of clusters.

**loglik** sample expected log-likelihood.

**size** cluster size (counts).

**cluster** cluster assignment based on the *maximum a posteriori* rule (MAP). Returned when `save_cluster = TRUE`.

**posterior** a matrix of dimension  $(N \times K)$  where `posterior[i, k]` is the estimated posterior probability that the *i*th observation belongs to the *k*th cluster. Returned when `save_taus = TRUE`.

**params** a list containing mixture component parameters. Returned when `save_params = TRUE`. The elements of the list are: `$proportion`= vector of proportions; `$mean`= matrix of dimension  $(P \times K)$  containing mean parameters; `$cov`= array of size  $(P \times P \times K)$  containing covariance matrices.

## References

Coretto, Pietro and Christian Hennig (2017). Consistency, breakdown robustness, and algorithms for robust improper maximum likelihood clustering. *Journal of Machine Learning Research*, Vol. 18(142), pp. 1-39. URL: <https://jmlr.org/papers/v18/16-382.html>

Coretto, Pietro and Christian Hennig (2023) Nonparametric consistency for maximum likelihood estimation and clustering based on mixtures of elliptically-symmetric distributions. *arXiv:2311.06108*. URL: <https://arxiv.org/abs/2311.06108>

## Examples

```
# --- load data
data("banknote")
dat <- banknote[-1]
n <- nrow(dat) # sample size
nc <- 2        # number of clusters

# fit 2 clusters using the default k-median initialization
set.seed(101)
fit1 <- gmix(dat, K = nc, init.nstart = 1)
print(fit1)

## Not run:
# plot partition (default)
plot(x = fit1, data = dat)

# plot partition onto the first 3 principal component coordinates
plot(x = fit1, data = prcomp(dat)$x, margins = c(1, 2, 3),
     pch_cl = c("A", "B"), col_cl = c("#4285F4", "#0F9D58"),
     main = "Principal Components")

## End(Not run)

# user-defined random initialization with hard assignment labels
set.seed(102)
i2 <- sample(1:nc, size = n, replace = TRUE)
fit2 <- gmix(dat, K = 2, init = i2)
## Not run:
plot(x = fit2, data = dat)

## End(Not run)

# user-defined smooth "toy" initialization:
# 50% of the points are assigned to cluster 1 with probability 0.9 and to
# cluster 2 with probability 0.1. The remaining data points are assigned to
# cluster 1 with probability 0.1 and to cluster 2 with probability 0.9.
set.seed(103)
idx <- sample(c(TRUE, FALSE), size = n, replace = TRUE)
i3 <- matrix(0, nrow = n, ncol = nc)
i3[idx, ] <- c(0.9, 0.1)
i3[!idx, ] <- c(0.1, 0.9)
fit3 <- gmix(dat, K = nc, init = i3)
```

```
## Not run:
plot(x = fit3, data = dat)

## End(Not run)

# user-defined function for initialization
# this one produces a 0-1 hard posterior matrix W based on kmeans
compute_init <- function(data, K){
  cl <- kmeans(data, K, nstart = 1, iter.max = 10)$cluster
  W <- sapply(seq(K), function(x) as.numeric(cl == x))
  return(W)
}
fit4 <- gmix(dat, K = nc, init = compute_init)
## Not run:
plot(fit4, data = dat)

## End(Not run)
```

---

mbind

*Combines Methods Settings*


---

## Description

The function combines functions containing clustering methods setups built using [mset\\_user](#) and related functions.

## Usage

```
mbind(...)
```

## Arguments

... one or more `qcmeth` objects obtained from [mset\\_user](#) and related functions, bare functions, or lists of bare functions. Bare functions are wrapped as unnamed user methods.

## Details

`mbind()` does not modify the supplied methods; it concatenates them into a single `qcmeth` object.

## Value

An S3 object of class `'qcmeth'`. Each element of the list represents a competing method containing the following objects

<code>fullname</code>	a string identifying the setup.
<code>callargs</code>	a list with arguments that are passed to the base function.

fn the function implementing the specified setting. This fn function can be executed on the data set. It has at least two arguments: data and only\_params. data is a data matrix or data.frame only\_params is logical. If only\_params==FALSE (default), fn will return the object returned by the underlying clustering method. If only\_params==TRUE (default) fn will return only cluster parameters (proportion, mean, and cov; see [clust2params](#)).

## References

Coraggio, Luca and Pietro Coretto (2023). Selecting the number of clusters, clustering models, and algorithms. A unifying approach based on the quadratic discriminant score. *Journal of Multivariate Analysis*, Vol. 196(105181), 1-20. doi: [doi:10.1016/j.jmva.2023.105181](https://doi.org/10.1016/j.jmva.2023.105181)

## See Also

[mset\\_user](#), [mset\\_gmix](#), [mset\\_kmeans](#), [mset\\_pam](#)

## Examples

```
# load data
data("banknote")
dat <- banknote[-1]

# generate kmeans setups
A <- mset_kmeans(K=c(2,3))

# generate gmix setups
B <- mset_gmix(K=c(2,3))

# combine setups
M <- mbind(A, B)

# get one combined setting
m <- M[[4]]
m

# cluster data with 'm'
fit <- m$fn(dat)
fit
```

---

mset\_gmix

*Generates Methods Settings for Gaussian Mixture Model-Based Clustering*

---

## Description

The function generates a software abstraction of a list of clustering models implemented through a set of tuned methods and algorithms. In particular, it generates a list of [gmix](#)-type functions each combining model tuning parameters and other algorithmic settings. The generated functions are ready to be called on the data set.

**Usage**

```
mset_gmix(
  K = seq(10),
  init = "kmed",
  erc = c(1, 50, 1000),
  iter.max = 1000,
  tol = 1e-08,
  init.nstart = 25,
  init.iter.max = 30,
  init.tol = tol
)
```

**Arguments**

<code>K</code>	a vector/list, specifies the number of clusters.
<code>init</code>	settings of the <code>init</code> parameter of <code>gmix</code> . This can be a character vector with elements in <code>c("kmed", "kmeans", "pam")</code> , a function, a matrix/data.frame of initial weights, or a list combining these. See <code>gmix</code> for the meaning of each initialization type.
<code>erc</code>	a vector/list, contains the settings of the <code>erc</code> parameter of <code>gmix</code> .
<code>iter.max</code>	a integer vector, contains the settings of the <code>iter.max</code> parameter of <code>gmix</code> .
<code>tol</code>	a vector/list, contains the settings of the <code>tol</code> parameter of <code>gmix</code> .
<code>init.nstart</code>	a integer vector, contains the settings of the <code>init.nstart</code> parameter of <code>gmix</code> .
<code>init.iter.max</code>	a integer vector, contains the settings of the <code>init.iter.max</code> parameter of <code>gmix</code> .
<code>init.tol</code>	a vector/list, contains the settings of the <code>init.tol</code> parameter of <code>gmix</code> .

**Details**

The function produces functions implementing competing clustering methods based on several Gaussian Mixture models specifications. The function produces functions for fitting competing Gaussian Mixture model-based clustering methods settings. This is a specialized version of the more general function `mset_user`. In particular, it produces a list of `gmix` functions each corresponding to a specific setup in terms of both model hyper-parameters (*e.g.* the number of clusters, the eigenvalue ratio constraint, *etc.*) and algorithm's control parameters (*e.g.* the type of initialization, maximum number of iteration, *etc.*). See `gmix` for a detailed description of the role of each argument and their data types.

Each combination of tuning parameters yields one element of the returned `qcmeth` object.

When `init` is a list, character, function, and matrix/data.frame initializations can be combined in the same `qcmeth` object.

**Value**

An S3 object of class `'qcmeth'`. Each element of the list represents a competing method containing the following objects

<code>fullname</code>	a string identifying the setup.
-----------------------	---------------------------------

`callargs` a list with `gmix` function arguments.

`fn` the function implementing the specified setting. This `fn` function can be executed on the data set. It has arguments `data`, `save_cluster`, `save_params`, `save_taus`, and `only_params`. `data` is a data matrix or `data.frame` and `only_params` is logical. If `only_params==FALSE` (default), `fn` will return the object returned by `gmix`. If `only_params==TRUE`, `fn` will return only cluster parameters (proportion, mean, and cov; see `clust2params`).

## References

Coraggio, Luca, and Pietro Coretto (2023). Selecting the Number of Clusters, Clustering Models, and Algorithms. A Unifying Approach Based on the Quadratic Discriminant Score. *Journal of Multivariate Analysis*, Vol. 196(105181), pp. 1-20, doi:[10.1016/j.jmva.2023.105181](https://doi.org/10.1016/j.jmva.2023.105181)

## See Also

[gmix](#), [mset\\_user](#), [bqs](#)

## Examples

```
# 'gmix' settings combining number of clusters K={3,4} and eigenvalue
# ratio constraints {1,10}
A <- mset_gmix(K = c(2,3), erc = c(1,10))

# select setup 1: K=2, erc = 1, init = "kmed"
ma1 <- A[[1]]
print(ma1)

# fit A[[1]] on banknote data
data("banknote")
dat <- banknote[-1]
fit1 <- ma1$fn(dat)
fit1

# if only cluster parameters are needed
fit1b <- ma1$fn(dat, only_params = TRUE)
fit1b

# include a custom initialization, see also help('gmix')
compute_init <- function(data, K){
  cl <- kmeans(data, K, nstart=1, iter.max=10)$cluster
  W <- sapply(seq(K), function(x) as.numeric(cl==x))
  return(W)
}

# generate methods settings
B <- mset_gmix(K = c(2,3), erc = c(1,10),
              init = list(compute_init, "kmed"))
```

```
# select setup 2: K=2, erc=10, init = compute_init
mb2 <- B[[2]]
fit2 <- mb2$fn(dat)
fit2
```

---

mset\_kmeans

*Generates Methods Settings for K-Means Clustering*


---

## Description

The function generates a software abstraction of a list of clustering models implemented through a set of tuned methods and algorithms. In particular, it generates a list of `kmeans`-type functions each combining tuning parameters and other algorithmic settings. The generated functions are ready to be called on the data set.

## Usage

```
mset_kmeans(
  K = c(1:10),
  iter.max = 50,
  nstart = 30,
  algorithm = "Hartigan-Wong",
  trace = FALSE
)
```

## Arguments

<code>K</code>	a vector, specifies the number of clusters.
<code>iter.max</code>	a vector, contains the settings of the <code>iter.max</code> parameter of <code>kmeans</code> .
<code>nstart</code>	a vector, contains the settings of the <code>nstart</code> parameter of <code>kmeans</code> .
<code>algorithm</code>	a vector, contains the settings of the <code>algorithm</code> parameter of <code>kmeans</code> .
<code>trace</code>	a vector, contains the settings of the <code>trace</code> parameter of <code>kmeans</code> .

## Details

The function produces functions implementing competing clustering methods based on the K-Means methodology as implemented in `kmeans`. This is a specialized version of the more general function `mset_user`. In particular, it produces a list of `kmeans` functions each corresponding to a specific setup in terms of hyper-parameters (*e.g.* the number of clusters) and algorithm's control parameters (*e.g.* initialization). See `kmeans` for a detailed description of the role of each argument and their data types.

Each combination of tuning parameters yields one element of the returned `qcmethod` object.

In the generated `fn`, the `params` component is built from the returned partition via `clust2params`.

**Value**

An S3 object of class 'qcmethod'. Each element of the list represents a competing method containing the following objects

fullname	a string identifying the setup.
callargs	a list with <a href="#">kmeans</a> function arguments.
fn	the function implementing the specified setting. This fn function can be executed on the data set. It has two arguments: data and only_params. data is a data matrix or data.frame only_params is logical. If only_params==FALSE (default), fn will return the object returned by <a href="#">kmeans</a> , augmented with a params component. If only_params==TRUE (default) fn will return only cluster parameters (proportion, mean, and cov; see <a href="#">clust2params</a> ).

**References**

Coraggio, Luca, and Pietro Coretto (2023). Selecting the Number of Clusters, Clustering Models, and Algorithms. A Unifying Approach Based on the Quadratic Discriminant Score. *Journal of Multivariate Analysis*, Vol. 196(105181), pp. 1-20, doi:[10.1016/j.jmva.2023.105181](https://doi.org/10.1016/j.jmva.2023.105181)

**See Also**

[kmeans](#), [mset\\_user](#), [bqs](#)

**Examples**

```
# 'kmeans' settings combining number of clusters K={2,3}
# and numbers of random starts {10,20}
A <- mset_kmeans(K = c(2,3), nstart = c(10,20))

# select setup 1: K=2, nstart = 10
m <- A[[1]]
print(m)

# cluster with the method set in 'm'
data("banknote")
dat <- banknote[-1]
fit1 <- m$fn(dat)
fit1
class(fit1)

# if only cluster parameters are needed
fit2 <- m$fn(dat, only_params = TRUE)
fit2
```

---

mset_pam	<i>Generates Methods Settings for Partitioning Around Medoids (Pam) Clustering</i>
----------	--

---

### Description

The function generates a software abstraction of a list of clustering models implemented through the a set of tuned methods and algorithms. In particular, it generates a list of `pam`-type functions each combining tuning parameters and other algorithmic settings. The generated functions are ready to be called on the data set.

### Usage

```
mset_pam(
  K = seq(10),
  metric = "euclidean",
  medoids = if (is.numeric(nstart)) "random",
  nstart = if (variant == "faster") 1 else NA,
  stand = FALSE,
  do.swap = TRUE,
  variant = "original",
  pamonce = FALSE
)
```

### Arguments

<code>K</code>	a vector/list, specifies the number of clusters.
<code>metric</code>	a vector, contains the settings of the <code>metric</code> parameter of <code>pam</code> .
<code>medoids</code>	settings of the <code>medoids</code> parameter of <code>pam</code> . This can be a character vector, a numeric vector of user-supplied medoid labels, or a list combining these.
<code>nstart</code>	a vector, contains the settings of the <code>nstart</code> parameter of <code>pam</code> .
<code>stand</code>	a vector, contains the settings of the <code>stand</code> parameter of <code>pam</code> .
<code>do.swap</code>	a vector, contains the settings of the <code>do.swap</code> parameter of <code>pam</code> .
<code>variant</code>	a list, contains the settings of the <code>variant</code> parameter of <code>pam</code> .
<code>pamonce</code>	a vector, contains the settings of the <code>pamonce</code> parameter of <code>pam</code> .

### Details

The function produces functions implementing competing clustering methods based on the PAM clustering methodology as implemented in `pam`. This is a specialized version of the more general function `mset_user`. In particular, it produces a list of `pam` functions each corresponding to a specific setup in terms of hyper-parameters (*e.g.* the number of clusters) and algorithm's control parameters (*e.g.* initialization). See `pam` for a detailed description of the role of each argument and their data types.

Each combination of tuning parameters yields one element of the returned `qcmeth` object.

When `medoids` is numeric or a list containing numeric entries, the corresponding number of clusters is derived from the supplied labels.

In the generated `fn`, the `params` component is built from the returned partition via [clust2params](#).

### Value

An S3 object of class `'qcmethod'`. Each element of the list represents a competing method containing the following objects

<code>fullname</code>	a string identifying the setup.
<code>callargs</code>	a list with <a href="#">pam</a> function arguments.
<code>fn</code>	the function implementing the specified setting. This <code>fn</code> function can be executed on the data set. It has arguments <code>data</code> , <code>diss</code> , <code>cluster.only</code> , <code>keep.data</code> , <code>keep.diss</code> , and <code>only_params</code> . <code>data</code> is a data matrix or <code>data.frame</code> and <code>only_params</code> is logical. If <code>only_params==FALSE</code> (default), <code>fn</code> will return the object returned by <a href="#">pam</a> , augmented with a <code>params</code> component. If <code>only_params==TRUE</code> (default) <code>fn</code> will return only cluster parameters (proportion, mean, and cov; see <a href="#">clust2params</a> ).

### References

Coraggio, Luca, and Pietro Coretto (2023). Selecting the Number of Clusters, Clustering Models, and Algorithms. A Unifying Approach Based on the Quadratic Discriminant Score. *Journal of Multivariate Analysis*, Vol. 196(105181), pp. 1-20, doi:[10.1016/j.jmva.2023.105181](https://doi.org/10.1016/j.jmva.2023.105181)

### See Also

[pam](#), [mset\\_user](#), [bqs](#)

### Examples

```
# 'pam' settings combining number of clusters K={2,3}, and dissimilarities {euclidean, manhattan}
A <- mset_pam(K = c(2,3), metric = c("euclidean", "manhattan"))

# select setup 1: K=2, metric = "euclidean"
m <- A[[1]]
print(m)

# cluster with the method set in 'm'
data("banknote")
dat <- banknote[-1]
fit1 <- m$fn(dat)
fit1
class(fit1)

# if only cluster parameters are needed
fit1b <- m$fn(dat, only_params = TRUE)
fit1b
```

---

mset_user	<i>Generates Clustering Methods Settings for a Prototype Methodology Provided by the User</i>
-----------	---

---

### Description

The function generates a software abstraction of a list of clustering models implemented through the a set of tuned methods and algorithms. The *base* clustering methodology is provided via a user-defined function. The latter prototype is expanded in a list of functions each combining tuning parameters and other algorithmic settings. The generated functions are ready to be called on the data set.

### Usage

```
mset_user(fname, .packages = NULL, .export = NULL, ...)
```

### Arguments

fname	the name of a function implementing a user-defined clustering method. It clusters a data set and outputs cluster parameters. fname must fulfill certain requirements detailed below in the <i>Details</i> .
.packages	character vector of packages that the tasks in fname depend on (see <i>Details</i> ).
.export	character vector of variables to export that are needed by fname and that are not defined in the current environment (see <i>Details</i> ).
...	parameters passed to fname. If a given parameter is included as a vector/list each of its members is to obtain the final collection of fname specifications (see <i>Details</i> and <i>Examples</i> ).

### Details

The function produces functions implementing competing clustering methods based on a *prototype* methodology implemented by the user via the input argument *fname*. In particular, it builds a list of *fname*-type functions each corresponding to a specific setup in terms of hyper-parameters (*e.g.* the number of clusters) and algorithm's control parameters (*e.g.* initialization).

Each combination of tuning parameters yields one element of the returned `qcmethod` object.

**Requirements for *fname*.** *fname* must be the name of a callable function implementing the base clustering method of interest. It must have the following input argument

- *data*: a numeric vector, matrix, or data frame of observations. Rows correspond to observations and columns correspond to variables/features. Categorical variables and NA values are not allowed.

Additionally, *fname* can have any other input parameter controlling the underlying clustering model/method/algorithm. All this additional parameters are passed to `mset_user` via `...` (see *Arguments*).

The output of *fname* must contain a list named `params` with cluster parameters describing size, centrality and scatter. Let  $P = \text{number of variable/features}$  and  $K = \text{number of clusters}$ . The elements of `params` are as follows:

- `proportion`: a vector of clusters' proportions;
- `mean`: a matrix of dimension  $(P \times K)$  containing the clusters' mean parameters;
- `cov`: an array of size  $(P \times P \times K)$  containing the clusters' covariance matrices.

Note that `params` can be easily obtained from a vector of cluster labels using `clust2params`.

`.packages` and `.export`. The user does not normally need to specify `.packages` and `.export`. These arguments are not needed if the functions generated by `mset_user` will be called from an environment containing all variables and functions needed to execute `fname`. Functions like `bqs` will call the functions generated by `mset_user` within a parallel infrastructure using `foreach`. If the user specifies `.packages` and `.export`, they will be passed to the `.packages` and `.export` arguments of `foreach`.

The generated `fn` returns `res$params` unchanged when `only_params = TRUE`.

Finally, note that the package already contains specialized versions of `mset_user` generating methods settings for some popular algorithms (see `mset_gmix`, `mset_kmeans`, `mset_pam`)

## Value

An S3 object of class `'qcmethod'`. Each element of the list represents a competing method containing the following objects

<code>fullname</code>	a string identifying the setup.
<code>callargs</code>	a list with arguments that are passed to the base function.
<code>fn</code>	the function implementing the specified setting. This <code>fn</code> function can be executed on the data set. It has two arguments: <code>data</code> and <code>only_params</code> . <code>data</code> is a data matrix or <code>data.frame</code> <code>only_params</code> is logical. If <code>only_params==FALSE</code> (default), <code>fn</code> will return the object returned by <code>fname</code> . If <code>only_params==TRUE</code> (default) <code>fn</code> will return only cluster parameters ( <code>proportion</code> , <code>mean</code> , and <code>cov</code> ; see <code>clust2params</code> ).

## References

Coraggio, Luca, and Pietro Coretto (2023). Selecting the Number of Clusters, Clustering Models, and Algorithms. A Unifying Approach Based on the Quadratic Discriminant Score. *Journal of Multivariate Analysis*, Vol. 196(105181), pp. 1-20, doi:10.1016/j.jmva.2023.105181

## See Also

`clust2params`, `mset_gmix`, `mset_kmeans`, `mset_pam`

## Examples

```
# load data
data("banknote")
dat <- banknote[-1]

# EXAMPLE 1: generate Hierarchical Clustering settings
# -----
```



```

    return(y)
  }

# generate 'mclust' model settings by varying the number of clusters and
# covariance matrix models (see help('mclust::mclustModelNames'))
B <- mset_user(fname = "mc_wrapper", K = c(2,3), modelNames = c("EEI", "VVV"))

# get the setting with K=3 and covariance model "EEI"
mb <- B[[2]]
mb

# cluster data with 'mb'
fit_b <- mb$fn(dat)
fit_b ## class(fit_b) = "Mclust"

# if needed one can make sure that 'mclust' package is always available
# by setting the argument '.packages'
B <- mset_user(fname = "mc_wrapper", K = c(2,3), modelNames = c("EEI","VVV"),
              .packages = c("mclust"))

## End(Not run)

## Not run:
# EXAMPLE 3: generate 'dbscan' settings
# -----
# DBSCAN is popular nonparametric method for discovering clusters of
# arbitrary shapes with noise. The number of clusters is implicitly
# determined via two crucial tunings usually called 'eps' and 'minPts'
# See https://en.wikipedia.org/wiki/DBSCAN
require(dbscan)

# wrapper for dbscan::dbscan
db_wrap <- function(data, ...) {
  cl <- dbscan(data, borderPoints = TRUE, ...)$cluster
  return(list(params = clust2params(data, cl)))
}

D <- mset_user(fname = "db_wrap", eps = c(0.5, 1), minPts=c(5,10))
md <- D[[2]]
fit_d <- md$fn(dat)
fit_d
class(fit_d)

## End(Not run)

```

**Description**

Produce a plot of bqs (Bootstrap Quadratic Scores). This function creates plots based on the BQS (Bootstrap Quality Scores) data.

**Usage**

```
## S3 method for class 'bqs'
plot(x, score = NULL, perc_scale = FALSE, top = NULL, annotate = NULL, ...)
```

**Arguments**

x	An S3 object of class bqs as returned by the <a href="#">bqs</a> function. x must be ranked, i.e. it must have a non-missing rankby component.
score	Character vector specifying the score(s) to be plotted. Valid scores are "hard", "smooth", "oob_hard", and "oob_smooth". If NULL (default), all score components available in x are plotted.
perc_scale	Logical; if TRUE, scales the plot using percentages, relative to the best score. Default is FALSE.
top	Numeric; specifies the number of top models to individually highlight. Must be a single number less than or equal to the length of x\$methodset. If NULL (default), top is automatically determined based on the score values. Top models are emphasized visually, not filtered.
annotate	Logical; if TRUE, annotates the top models in the plot. Default is automatically determined (TRUE if the number of methods M <= 30, FALSE otherwise). Annotations include method names and plotted score values.
...	Further arguments passed to or from other methods.

**Details**

The annotate argument is mainly intended to control built-in labels, but setting it to FALSE also leaves more room for expert users to add custom annotations after the plot is drawn.

**Value**

No return value, called for side effects.

**See Also**

[bqs](#)

**Examples**

```
# load data
data("banknote")
dat <- banknote[-1]

# set up methods
mlist <- mset_gmix(K = 1:3, erc = c(1, 100))
```

```

# perform bootstrap
# change B and ncores to a much larger value in real problems
res <- bqs(dat, mlist, B = 3, type = "both", rankby = "lq",
          ncores = 1, oob = TRUE, savescores = FALSE, saveparams = FALSE)

# Plot with default settings
plot(res)

# Plot in percentage scale relative to first model
plot(res, perc_scale = TRUE)

```

---

plot.mbcfit

*Plot Fitted Mixture Models*


---

### Description

This function provides a plot method for objects of class `mbcfi`t, returned as output by the `gmix` function. It serves as a wrapper around `plot_clustering`, allowing easy visualization of clustering results, including clustering assignments, contours, and boundaries.

### Usage

```

## S3 method for class 'mbcfi't
plot(
  x,
  data = NULL,
  subset = NULL,
  what = c("clustering", "contour"),
  col_cl = NULL,
  pch_cl = NULL,
  ...
)

```

### Arguments

<code>x</code>	An object of class <code>mbcfi</code> t, typically a result of the <code>gmix</code> function.
<code>data</code>	NULL or a data matrix, data frame, or array containing data points to be plotted. When supplied, it is typically the data set used to fit <code>x</code> . See <i>Details</i> .
<code>subset</code>	A numeric vector indexing columns of data to subset and focus the plot on specific features. Default is NULL.
<code>what</code>	Character vector specifying which elements to plot. Options are "clustering", "contour", and "boundary". Default is to plot "clustering" and "contour". Unavailable plot features are ignored or rejected downstream by <code>plot_clustering</code> depending on the inputs. See <i>Details</i> .

col_cl	A vector of colors to use for clusters (one for each cluster). Default is NULL, which uses a default sequence of colors.
pch_cl	A vector of plotting symbols (one for each cluster) to use for clusters. Default is NULL, which uses a default sequence of symbols.
...	Further arguments passed to or from other methods.

### Details

The `plot.mbcfit` function provides a plotting method for objects of class `mbcfi`. It acts as a wrapper around the `plot_clustering` function, allowing users to easily generate various plots to analyze the clustering results. A plot is produced only upon a successful `mbcfi` estimate, i.e., when `mbcfi` has code equal to either 1 or 2. The plot features that can actually be drawn depend on the components stored in `x`, in particular `x$params` and `x$cluster`.

When data is NULL (the default), the function constructs a synthetic plotting data set from the fitted params and then delegates the plotting to `plot_clustering`.

When data is not NULL, the function passes data, the stored mixture parameters, and the hard clustering labels saved in `x$cluster` to `plot_clustering`.

### Value

Called for its side effects.

### See Also

`gmix`, `plot_clustering`, `predict.mbcfit`

### Examples

```
# load data
data("banknote")
dat <- banknote[-1]

# fit 2 clusters
set.seed(123)
fit <- gmix(dat, K = 2, init.nstart = 1)
print(fit)

# plot partition (default)
plot(x = fit, data = dat)

# plot partition onto the first 3 coordinates
plot(x = fit, data = dat, subset = c(1:3), pch_cl = c("A", "B"),
     col_cl = c("#4285F4", "#0F9D58"), what = "clustering")

# additionally plot clustering boundary and contour sets
plot(x = fit, data = dat, subset = c(1:3), pch_cl = c("A", "B"),
     col_cl = c("#4285F4", "#0F9D58"),
     what = c("clustering", "boundary", "contour"))
```

---

plot\_clustering      *Plot Data With Clustering Information*

---

### Description

This function plots data and optionally adds clustering information such as clustering assignments, contours, or boundaries.

### Usage

```
plot_clustering(
  data,
  subset = NULL,
  cluster = NULL,
  params = NULL,
  what = c("clustering", "contour", "boundary"),
  col_cl = NULL,
  pch_cl = NULL
)
```

### Arguments

data	a numeric vector, matrix, or data frame of observations. Rows correspond to observations and columns correspond to variables/features. Categorical variables and NA values are not allowed.
subset	A numeric vector indexing columns of data to be visualized. Default is NULL.
cluster	A vector of cluster assignments. If provided, the plot can display clustering information as specified in what. Must have the same number of observations as data.
params	A list of clustering parameters, including proportion, mean, and cov. If provided, the plot can display contour and boundary information. For "contour" and "boundary", params must be valid mixture parameters.
what	Character vector specifying which elements to plot. Options are "clustering", "contour", and "boundary". The default request is all three. Requested features that are incompatible with the supplied inputs are dropped with a warning; if none remain, the function stops with an error.
col_cl	A vector of colors to use for clusters (one for each cluster). Default is NULL, which uses a default sequence of colors.
pch_cl	A vector of plotting symbols (one for each cluster) to use for clusters. Default is NULL, which uses a default sequence of symbols.

## Details

At least one of `cluster` or `params` must be supplied. Contours and boundaries require Gaussian-ready parameters. Depending on the data dimension, the function produces one-dimensional plots, two-dimensional plots, or a scatterplot matrix over feature pairs. When `subset` is used, `params` are restricted to the selected coordinates before plotting.

## Value

No return value, called for side effects.

## See Also

[bqs](#), [clust2params](#)

## Examples

```
# Example data
set.seed(123)
data <- rbind(
  matrix(rnorm(100 * 2), ncol = 2),
  matrix(rnorm(100 * 2) + 2, ncol = 2)
)
cluster <- c(rep(1, 100), rep(2, 100))
params <- clust2params(data, cluster)

# Plot with clustering information
plot_clustering(data, cluster = cluster, what = "clustering")

# Plot with subset of variables
plot_clustering(data, cluster = cluster, subset = 1,
  what = c("clustering", "contour"))

# Plot with customized colors and symbols
plot_clustering(data, cluster = cluster, params = params,
  col_cl = c("magenta", "orange"),
  pch_cl = c("A", "B"))
```

---

predict.mbcfit

*Predict Hard Clustering Assignments for using Mixture Models*

---

## Description

This function predicts cluster assignments for new data based on an existing model of class `mbcfit`. The prediction leverages information from the fitted model to categorize new observations into clusters.

**Usage**

```
## S3 method for class 'mbcfite'
predict(object, newdata, ...)
```

**Arguments**

**object** An object of class `mbcfite`, representing the fitted mixture model. This is typically obtained in output from the `gmix` function. See *Details*.

**newdata** A numeric vector, matrix, or data frame of observations. Rows correspond to observations and columns correspond to variables/features. Categorical variables and NA values are not allowed. The number of columns must be coherent with that implied by `object`. See *Details*.

**...** Further arguments passed to or from other methods.

**Details**

The `predict.mbcfit` function utilizes the parameters of a previously fitted `mbcfite` model to allocate new data points to estimated clusters. The function performs necessary checks to ensure the `mbcfite` model returns valid estimates and the dimensionality of the new data aligns with the model. The `mbcfite` object must contain a component named `params`, which is itself a list containing the following necessary elements, for a mixture model with  $K$  components:

**proportion** A numeric vector of length  $K$ , with elements summing to 1, representing cluster proportions.

**mean** A numeric matrix of dimensions  $c(P, K)$ , representing cluster centers.

**cov** A numeric array of dimensions  $c(P, P, K)$ , representing cluster covariance matrices.

Data dimensionality is  $P$ , and new data dimensionality must match (`ncol(newdata)` must be equal to  $P$ ) or otherwise the function terminates with an error message. The stored mixture parameters must be Gaussian-ready, i.e. proportions must be positive and sum to 1, and covariance matrices must be finite, symmetric, and positive definite.

The predicted clustering is obtained as the MAP estimator using posterior weights of a Gaussian mixture model parametrized at `params`. Denoting with  $z(x)$  the predicted cluster label for point  $x$ , and with  $\phi$  the (multivariate) Gaussian density:

$$z(x) = \arg \max_{k=\{1, \dots, K\}} \frac{\pi_k \phi(x, \mu_k, \Sigma_k)}{\sum_{j=1}^K \pi_j \phi(x, \mu_j, \Sigma_j)}$$

**Value**

A vector of predicted cluster labels, one for each observation in `newdata`.

**References**

Coraggio, Luca and Pietro Coretto (2023). Selecting the number of clusters, clustering models, and algorithms. A unifying approach based on the quadratic discriminant score. *Journal of Multivariate Analysis*, Vol. 196(105181), 1-20. doi: [doi:10.1016/j.jmva.2023.105181](https://doi.org/10.1016/j.jmva.2023.105181)

**See Also**[gmix](#)**Examples**

```
# load data
data(banknote)
dat <- banknote[, -1]

# Estimate 3-components gaussian mixture model
set.seed(123)
res <- gmix(dat, K = 3)

# Cluster in output from gmix
print(res$cluster)

# Predict cluster on a single point
# (keep table dimension)
predict(res, dat[1, , drop = FALSE])

# Predict cluster on a subset
predict(res, dat[1:10, ])

# Predicted cluster on original dataset are equal to the clustering from the
# gmix model
all(predict(res, dat) == res$cluster)
```

---

print.bqs

*Display Information on Bootstrap Quadratic Scores Objects*

---

**Description**

This function provides a print method for objects of class `bqs`, which are produced by the `bqs` function. It prints a summary of the bootstrapped quadratic score results for the clustering solutions considered.

**Usage**

```
## S3 method for class 'bqs'
print(x, ...)
```

**Arguments**

`x` An object of class `bqs`, usually the output of the `bqs` function.  
`...` Additional arguments passed to or from other methods.

## Details

The `print.bqs` function provides a `print` method for objects of class `bqs`.

If clustering solutions in `bqs` are not ranked, the printing method displays a message to the user signalling it. Otherwise, the printing method shows a summary of the top-6 ranked solutions, in increasing rank order, for any available scoring method. The available scoring methods are determined by the `type` and `oob` arguments used in input to the `bqs` function (see Details in [bqs](#)).

The summary tables for ranked methods has `row.names` set to the method's codename, and shows the following information along the columns:

`id` Method's index in the methodset list (see Details in [bqs](#)).

`rank` Method's rank according to ranking criterion.

`score` (Only shown when `B=0`) Method's quadratic score on the full data.

`mean` (Only shown when `B>0`) Method's mean bootstrap quadratic score.

`sterr` (Only shown when `B>0`) Method's standard error for the bootstrap quadratic score.

`lower_qnt` (Only shown for "mean" and "1q" ranking, when `B>0`) Method's lower  $\alpha/2$ -level quantile of the bootstrap distribution of the quadratic score (`alpha` is given in input to `bqs` function).

`upper_qnt` (Only shown for "mean" and "1q" ranking, when `B>0`) Method's upper  $\alpha/2$ -level quantile of the bootstrap distribution of the quadratic score (`alpha` is given in input to `bqs` function).

`-1se` (Only shown for "1se" ranking, when `B>0`) Method's mean bootstrap quadratic score minus 1 standard error.

`+1se` (Only shown for "1se" ranking, when `B>0`) Method's mean bootstrap quadratic score plus 1 standard error.

Methods with missing ranks are omitted from the printed summary. If all ranks are missing for a given score component, a short message is printed instead of a table.

## Value

No return value, called for side effects.

## See Also

[bqs](#), [bqs\\_rank](#)

## Examples

```
# Load data and set seed
set.seed(123)
data("banknote")
dat <- banknote[-1]

# set up kmeans, see help('mset_kmeans')
KM <- mset_kmeans(K = 2:5)

# set up Gaussian model-based clustering via gmix()
```

```

GMIX <- mset_gmix(K=2:5, erc=c(1, 50 , 100))

# combine tuned methods
mlist <- mbind(KM, GMIX)

# perform bootstrap
# se 'ncores' to the number of available physical cores
res <- bqs(dat, mlist, B = 100, type = "both", rankby=NA, ncores = 1,
          oob = TRUE, savescores = TRUE, saveparams = FALSE)

# Methods are not ranked; only available components are shown
res

# Rank method and show summaries
ranked_res <- bqs_rank(res, rankby = "lq", boot_na_share = 0.25)

ranked_res

```

---

print.mbcfit

*Display Information for Mixture Model Objects*


---

### Description

This function provides a print method for objects of class `mbcf`, returned in output by the `gmix` function.

### Usage

```

## S3 method for class 'mbcf'
print(x, ...)

```

### Arguments

`x` An object of class `mbcf`, typically a result of the `gmix` function.

`...` Further arguments passed to or from other methods.

### Details

The `print.mbcfit` function gives a summary of a model-based clustering fit, estimated using the `gmix` function.

The printed message depends on `x$info$code`:

- 2 'Lapack DSYEV failed'. This error occurs whenever any of the cluster-covariance matrices becomes singular during estimation, using the EM algorithm.
- 1 'Memory allocation error'. This error occurs when there is insufficient available memory to allocate the quantities required to execute the EM algorithm.

- 1 Success.
- 2 'gmix' did not converge (iterations reached the maximum limit).
- 3 EM algorithm failed; no better than the initial solution. This error occurs whenever the EM algorithm failed for other reasons (e.g., degenerate posterior-weights could not be prevented), and it was not possible to find a solution.

The printed output also lists available components of the `mbcf it` object and summarizes the number of clusters found and their size, whenever this information is available.

### Value

No return value, called for side effects.

### See Also

[gmix](#)

### Examples

```
set.seed(123)

# Estimate a 3-clusters Gaussian mixture model, using iris data as example
res <- gmix(iris[, -5], K = 3, erc = 10)

# Print the 'gmix' output
print(res)
```

---

qcluster

*qcluster: Clustering via Quadratic Scoring*

---

### Description

`qcluster` provides tools for tuning clustering models, methods, and algorithms by quadratic scoring with resampling.

### Details

The package combines three main components:

- method generators such as [mset\\_user](#), [mset\\_gmix](#), [mset\\_kmeans](#), [mset\\_pam](#), and [mbind](#);
- bootstrap quadratic-score estimation, ranking, and selection through [bqs](#), [bqs\\_rank](#), and [bqs\\_select](#);
- direct Gaussian model-based clustering and scoring via [gmix](#) and [qscore](#).

A typical workflow is:

1. define a collection of candidate clustering methods with `mset_*`() and optionally combine them with [mbind](#);

2. estimate bootstrap quadratic scores with `bqs`;
3. rank candidate methods with `bqs_rank` and extract selected full-data refits with `bqs_select`.

The package also provides plotting and printing methods for fitted `mbcf` and `bqs` objects, together with the sample data set `banknote`.

### Author(s)

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### References

Coraggio, Luca and Pietro Coretto (2023). Selecting the number of clusters, clustering models, and algorithms. A unifying approach based on the quadratic discriminant score. *Journal of Multivariate Analysis*, Vol. 196(105181), 1-20. doi: [doi:10.1016/j.jmva.2023.105181](https://doi.org/10.1016/j.jmva.2023.105181)

### See Also

Useful links:

- <https://luca-coraggio.com>
- <https://pietro-coretto.github.io>

---

qscore

*Clustering Quadratic Score*

---

### Description

Computes both the hard and the smooth quadratic score of a clustering.

### Usage

```
qscore(data, params, type = "both")
```

### Arguments

<code>data</code>	a numeric vector, matrix, or data frame of observations. Rows correspond to observations and columns correspond to variables/features. Let $N = \text{nrow}(\text{data})$ and $P = \text{ncol}(\text{data})$ . Categorical variables and NA values are not allowed.
<code>params</code>	a list containing cluster parameters ( <i>proportion</i> , <i>mean</i> , <i>cov</i> ). Let $K = \text{number of clusters}$ . The elements of the list are as follows: <code>\$proportion</code> = vector of clusters' proportions; <code>\$mean</code> = matrix of dimension $(P \times K)$ containing the clusters' mean parameters; <code>\$cov</code> = array of size $(P \times P \times K)$ containing the clusters' covariance matrices. These parameters must be conformable with <code>data</code> ; see also <a href="#">clust2params</a> .
<code>type</code>	the type of score, a character in the set $c(\text{"both"}, \text{"smooth"}, \text{"hard"})$ . The default value is set to <code>"both"</code> . See <i>Details</i> .

**Details**

The function calculates quadratic scores as defined in equation (22) in Coraggio and Coretto (2023). The score is computed from a Gaussian parameterization supplied in `params`.

**Value**

A named numeric vector with components `hard` and `smooth`. When only one score is requested through `type`, the other component is returned as `NA`.

**References**

Coraggio, Luca and Pietro Coretto (2023). Selecting the number of clusters, clustering models, and algorithms. A unifying approach based on the quadratic discriminant score. *Journal of Multivariate Analysis*, Vol. 196(105181), 1-20. DOI: [doi:10.1016/j.jmva.2023.105181](https://doi.org/10.1016/j.jmva.2023.105181)

**See Also**

[clust2params](#), [gmix](#)

**Examples**

```
# --- load and split data
data("banknote")
set.seed(345)
idx  <- sample(1:nrow(banknote), size = 25, replace = FALSE)
dat_f <- banknote[-idx, -1] ## training data set
dat_v <- banknote[ idx, -1] ## validation data set

# --- Gaussian model-based clustering, K=3
# fit clusters
fit1 <- gmix(dat_f, K = 3)
## compute quadratic scores using fitted mixture parameters
s1 <- qscore(dat_v, params = fit1$params)
s1

# --- k-means clustering, K=3
# obtain the k-means partition
cl_km <- kmeans(dat_f, centers = 3, nstart = 1)$cluster
## convert k-means hard assignment into cluster parameters
par_km <- clust2params(dat_f, cl_km)
# compute quadratic scores
s2 <- qscore(dat_v, params = par_km)
s2
```

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